

University of International Business and Economics International Summer School

MAT 120 Calculus II

Term: May 24 -June 24, 2021 Instructor: Sema Salur Home Institution: University of Rochester Email: semasalur@gmail.com Class Hours: Monday through Thursday, 120 minutes each day (2,400 minutes in total) Office hours: to be announced Discussion sessions: TBD

Total Contact Hours: 64 contact hours (45 minutes each, 48 hours in total) Location: WEB Credit: 4 units

Course Description:

In this course, the student will gain knowledge of the basic theory of integrals and proficiency with various standard techniques of integration: integration by parts, trigonometric substitution, partial fraction decomposition, etc. The student will also be exposed to certain traditional applications of those techniques: calculation of volumes (of solids of revolution, for example) and arc lengths, and the solution of some elementary differential equations. The student will be introduced to the theory of sequences and series, and the approximation of functions using series.

Course Goals:

A student who satisfactorily completes this course will:

- Have facility with the basic theory and techniques of integral calculus (the Fundamental Theorem of Calculus, integration by parts, etc.) and have an understanding of why the theory and techniques are valid.
- Have precise knowledge of the definitions and theorems from the basic theory of sequences and series: convergence of sequences, partial sums, series convergence, absolute convergence, conditional convergence, Integral Test, Comparison Test, etc.
- Have facility with basic calculational skills: evaluation of integrals using the basic techniques
 of integral calculus, calculation of volumes and arc length, solution of elementary differential
 equations, determination of convergence or divergence of sequences and series, calculation
 of radius of convergence of power series, determination of the power series representation
 of appropriate functions, etc.
- Have a rudimentary ability to explain mathematical theory (e.g., why integration by parts works, etc.) using rigorous mathematical reasoning.



Required Text:

Stewart, James. Single Variable Calculus: 8th edition with ISBN 978-1-285-74062-1

Prerequisites:

The course is based on Calculus I or its equivalent. Students are expected to know basic concepts of calculus for functions of a single real variable. They include: basic elementary functions and their properties, differentiation and geometrical significance of the derivative, definite and indefinite integrals, Fundamental Theorem of Calculus, indefinite integrals of basic elementary functions.

Attendance:

Students are expected to be present at all class meetings and examinations.

Grading Policy:

There will be one midterm and a final exam in this class. All exams will be closed-book. No notes, calculators, or other electronic devices will be allowed. and having such a device in view during the exam is an academic honesty violation.

The course grades will be calculated based on the following percentages:

- Homework: 30%
- Midterm: 30%
- Final Exam: 40%

The final exam will be cumulative. There will be no make-up exams.

Grading Scale:

Assignments and examinations will be graded according to the following grade scale:

Α	90-100	C+	72-74
A-	85-89	С	68-71
B+	82-84	C-	64-67
В	78-81	D	60-63
В-	75-77	F	below 60

Class Rules:

All academic work should be done with the high level of honesty and integrity. Academic misconduct of any kind may result in a grade penalty or the assignment of a failing grade.

Course Schedule:

Week 1

Assignment

The Fundamental Theorem of Calculus 4.3: 3, 7, 9, 11, 13, 19, 25, 29, 39, 49 The Substitution Rule



4.5: 3, 5, 7, 11, 17, 25, 37, 39, 41, 47 Areas between Curves 5.1: 1, 3, 5, 7, 13, 17, 21, 27, 29, 31 Volumes 5.2: 1, 3, 5, 7, 9, 11, 13, 15, 17, 19, 21 Volumes by Cylindrical Shells 5.3: 3, 7, 9, 11, 13, 15, 17, 19, 21, 29 Applications to Physics, Work 5.4: 1, 3, 5, 7, 11, 13, 15, 17, 21, 25 Average Value of a Function 5.5: 1, 3, 5, 7, 9, 11, 13, 15, 17, 19

Week 2

Assignment

Integration by Parts 7.1: 5, 7, 9, 11, 15, 17, 19, 21, 29, 37 Trigonometric Integrals 7.2: 3, 5, 11, 15, 19, 21, 23, 33, 45, 49 Trigonometric Substitution 7.3: 3, 5, 9, 11, 13, 19, 21, 23, 27, 29 Integration of Rational Functions by Partial Fractions 7.4: 5, 7, 9, 11, 15, 23, 27, 31, 39, 41 Strategy for Integration 7.5: 3, 11, 17, 23, 27, 35, 43, 49, 61, 63

Week 3

Assignment

Midterm Tuesday, June 8.

Improper Integrals 7.8: 1, 5, 7, 9, 11, 13, 21, 25, 27, 37 Arc Length 8.1: 3, 9, 11, 13, 17, 19, 21 Area of a Surface of Revolution 8.2: 3, 5, 7, 9, 11, 15 Curves Defined by Parametric Equations 10.1: 1, 5, 7, 9, 11, 15, 19 Calculus with Parametric Curves 10.2: 1, 3, 5, 7, 9, 11, 17

Week 4

Assignment

Polar Coordinates 10.3: 1, 3, 5, 7, 9, 11, 15, 17, 21, 29 Areas and Lengths in Polar Coordinates



10.4: 3, 7, 11, 13, 19, 23, 27, 29, 37, 39 Sequences 11.1: 3, 5, 7, 11, 15, 23, 25, 29, 31, 37 Series 11.2: 7, 15, 17, 19, 21, 25, 29, 22, 37, 43 The Integral Test 11.3: 3, 5, 7, 9, 11, 15, 17, 19, 21, 23, 25 The Comparison Tests 11.4: 3, 5, 7, 9, 11, 15, 17, 19, 21, 25, 29 Alternating Series 11.5: 3, 5, 9, 11, 19, 23, 25, 27, 29, 31, 33

Week 5 Assignment

Absolute Convergence, Ratio Test and Root Test 11.6: 3, 5, 7, 9, 11, 15, 17, 19, 21, 23, 25, 27, 29 Strategy for Testing Series 11.7: 1, 3, 5, 7, 9, 11, 13, 15, 17, 19, 21, 23, 25, 33, 37 Power Series 11.8: 3, 5, 7, 9, 11, 13, 15, 17, 19, 21, 23, 25 Representation of Functions as Power Series 11.9: 3, 5, 7, 9, 11, 15, 17, 19 Taylor and MacLaurin Series 11.10: 5, 11, 21, 35, 53, 61

Final Exam, June 24.

General Comments:

1. In order to train your minds in mathematical thinking, much of lecture will consist of the "Socratic Method" of questioning. Even if silently, do try to puzzle out the answers. An analogy: the lecture should be a "mental exercise" class. Knowledge cannot be given: it must be stolen. Engage your mind.

2. Many problems will not be solvable at first (or second) viewing. Be patient: clarify any unknown concepts, try to reduce the problem, brainstorm to unearth possibly relevant concepts, and follow your intuition. It may help to, after a period of hard work, put the problem away. Do not worry if you cannot do every problem: what is important is that you try.

3. If you find yourself getting lost in the material, come to office hours immediately! It is much is easier to lead a student's mind individually rather than in a group.

4. Note that we may not dot every i or cross every t in class: you are responsible for reading the text. In particular, it is to your advantage to read the material before coming to class; in this way the student becomes an active participant rather than a passive recipient.



5. Basic etiquette should be maintained. For example: to give your classmates time to think, please do not blurt out answers unless called upon (or overcome with excitement); please do not walk out of class without prior explanation, etc.

6. Using a cell phone in class is not permitted; students using phones will be penalized 5 percentage points on the next exam.

7. Tests will check your understanding of the lectures as well as cover homework-type problems; it will benefit you to check after each lecture to see if you've understood the line of the arguments. Precise knowledge of the theory is vital!