



**University of International Business and Economics  
International Summer School**

**MAT 120 Calculus II**

**Term: June 13<sup>th</sup> – July 14<sup>th</sup>, 2022**

**Instructor: LU Wanzhong**

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**Class Hours: Monday through Thursday, 120 minutes each day (2,400 minutes in total)**

**Office hours: TBD**

**Discussion sessions: 2 hours each week**

**Total Contact Hours: 64 contact hours (45 minutes each, 48 hours in total)**

**Location: WEB**

**Credit: 4 units**

**Course Description:**

In this course, the student will gain knowledge of the basic theory of integrals and proficiency with various standard techniques of integration: integration by parts, trigonometric substitution, partial fraction decomposition, etc. The student will also be exposed to certain traditional applications of those techniques: calculation of volumes (of solids of revolution, for example) and arc lengths, and the solution of some elementary differential equations. The student will be introduced to the theory of sequences and series, and the approximation of functions using series.

**Course Goals:**

**A student who satisfactorily completes this course will:**

- Have facility with the basic theory and techniques of integral calculus (the Fundamental Theorem of Calculus, integration by parts, etc.) and have an understanding of why the theory and techniques are valid.
- Have precise knowledge of the definitions and theorems from the basic theory of sequences and series: convergence of sequences, partial sums, series convergence, absolute convergence, conditional convergence, Integral Test, Comparison Test, etc.
- Have facility with basic calculational skills: evaluation of integrals using the basic techniques of integral calculus, calculation of volumes and arc length, solution of elementary differential equations, determination of convergence or divergence of sequences and series, calculation of radius of convergence of power series, determination of the power series representation of appropriate functions, etc.
- Have a rudimentary ability to explain mathematical theory (e.g., why integration by parts works, etc.) using rigorous mathematical reasoning.



**Required Text:**

Stewart, James. Single Variable Calculus: 8th edition with ISBN 978-1-285-74062-1

**Prerequisites:**

The course is based on Calculus I or its equivalent. Students are expected to know basic concepts of calculus for functions of a single real variable. They include: basic elementary functions and their properties, differentiation and geometrical significance of the derivative, definite and indefinite integrals, Fundamental Theorem of Calculus, indefinite integrals of basic elementary functions.

**Attendance:**

Students are expected to be present at all class meetings and examinations.

**Grading Policy:**

There will be one midterm and a final exam in this class. All exams will be closed-book. No notes, calculators, or other electronic devices will be allowed. and having such a device in view during the exam is an academic honesty violation.

The course grades will be calculated based on the following percentages:

- Homework: 30%
- Midterm: 30%
- Final Exam: 40%

The final exam will be cumulative. There will be no make-up exams.

**Grading Scale:**

Assignments and examinations will be graded according to the following grade scale:

<b>A</b>	90-100	<b>C+</b>	72-74
<b>A-</b>	85-89	<b>C</b>	68-71
<b>B+</b>	82-84	<b>C-</b>	64-67
<b>B</b>	78-81	<b>D</b>	60-63
<b>B-</b>	75-77	<b>F</b>	below 60

**Class Rules:**

All academic work should be done with the high level of honesty and integrity. Academic misconduct of any kind may result in a grade penalty or the assignment of a failing grade.

**Course Schedule:**

**Week 1  
Assignment**

The Fundamental Theorem of Calculus  
4.3: 3, 7, 9, 11, 13, 19, 25, 29, 39, 49  
The Substitution Rule



4.5: 3, 5, 7, 11, 17, 25, 37, 39, 41, 47

Areas between Curves

5.1: 1, 3, 5, 7, 13, 17, 21, 27, 29, 31

Volumes

5.2: 1, 3, 5, 7, 9, 11, 13, 15, 17, 19, 21

Volumes by Cylindrical Shells

5.3: 3, 7, 9, 11, 13, 15, 17, 19, 21, 29

Applications to Physics, Work

5.4: 1, 3, 5, 7, 11, 13, 15, 17, 21, 25

Average Value of a Function

5.5: 1, 3, 5, 7, 9, 11, 13, 15, 17, 19

**Week 2  
Assignment**

Integration by Parts

7.1: 5, 7, 9, 11, 15, 17, 19, 21, 29, 37

Trigonometric Integrals

7.2: 3, 5, 11, 15, 19, 21, 23, 33, 45, 49

Trigonometric Substitution

7.3: 3, 5, 9, 11, 13, 19, 21, 23, 27, 29

Integration of Rational Functions by Partial Fractions

7.4: 5, 7, 9, 11, 15, 23, 27, 31, 39, 41

Strategy for Integration

7.5: 3, 11, 17, 23, 27, 35, 43, 49, 61, 63

**Week 3  
Assignment**

Midterm Tuesday, June 28.

Improper Integrals

7.8: 1, 5, 7, 9, 11, 13, 21, 25, 27, 37

Arc Length

8.1: 3, 9, 11, 13, 17, 19, 21

Area of a Surface of Revolution

8.2: 3, 5, 7, 9, 11, 15

Curves Defined by Parametric Equations

10.1: 1, 5, 7, 9, 11, 15, 19

Calculus with Parametric Curves

10.2: 1, 3, 5, 7, 9, 11, 17

**Week 4  
Assignment**

Polar Coordinates

10.3: 1, 3, 5, 7, 9, 11, 15, 17, 21, 29

Areas and Lengths in Polar Coordinates



10.4: 3, 7, 11, 13, 19, 23, 27, 29, 37, 39

Sequences

11.1: 3, 5, 7, 11, 15, 23, 25, 29, 31, 37

Series

11.2: 7, 15, 17, 19, 21, 25, 29, 22, 37, 43

The Integral Test

11.3: 3, 5, 7, 9, 11, 15, 17, 19, 21, 23, 25

The Comparison Tests

11.4: 3, 5, 7, 9, 11, 15, 17, 19, 21, 25, 29

Alternating Series

11.5: 3, 5, 9, 11, 19, 23, 25, 27, 29, 31, 33

### Week 5 Assignment

Absolute Convergence, Ratio Test and Root Test

11.6: 3, 5, 7, 9, 11, 15, 17, 19, 21, 23, 25, 27, 29

Strategy for Testing Series

11.7: 1, 3, 5, 7, 9, 11, 13, 15, 17, 19, 21, 23, 25, 33, 37

Power Series

11.8: 3, 5, 7, 9, 11, 13, 15, 17, 19, 21, 23, 25

Representation of Functions as Power Series

11.9: 3, 5, 7, 9, 11, 15, 17, 19

Taylor and MacLaurin Series

11.10: 5, 11, 21, 35, 53, 61

Final Exam, July 14.

#### General Comments:

1. In order to train your minds in mathematical thinking, much of lecture will consist of the “Socratic Method” of questioning. Even if silently, do try to puzzle out the answers. An analogy: the lecture should be a “mental exercise” class. Knowledge cannot be given: it must be stolen. Engage your mind.
2. Many problems will not be solvable at first (or second) viewing. Be patient: clarify any unknown concepts, try to reduce the problem, brainstorm to unearth possibly relevant concepts, and follow your intuition. It may help to, after a period of hard work, put the problem away. Do not worry if you cannot do every problem: what is important is that you try.
3. If you find yourself getting lost in the material, come to office hours immediately! It is much easier to lead a student’s mind individually rather than in a group.
4. Note that we may not dot every i or cross every t in class: you are responsible for reading the text. In particular, it is to your advantage to read the material before coming to class; in this way the student becomes an active participant rather than a passive recipient.



5. Basic etiquette should be maintained. For example: to give your classmates time to think, please do not blurt out answers unless called upon (or overcome with excitement); please do not walk out of class without prior explanation, etc.
6. Using a cell phone in class is not permitted; students using phones will be penalized 5 percentage points on the next exam.
7. Tests will check your understanding of the lectures as well as cover homework-type problems; it will benefit you to check after each lecture to see if you've understood the line of the arguments. Precise knowledge of the theory is vital!